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Electric vehicle demand estimation and charging station allocation using urban informatics

--Manuscript Draft--

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1 **Electric vehicle demand estimation and charging station allocation using urban informatics**

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33

1 **ABSTRACT**

2 This paper performs a novel data-driven approach to optimize electric vehicle (EV) public
3 charging. We translate the study area into a directed graph by partitioning it into discrete grids. A
4 modified geographical PageRank (MGPR) model is developed to estimate EV charging demand,
5 built upon trip origin-destination (OD) and social dimension features, and validated against real-
6 world charging data. The results are fed into the capacitated maximal coverage location problem
7 (CMCLP) model to optimize the spatial layout of public charging stations by maximizing their
8 utilization. It is shown that MGPR can effectively quantify the EV charging demand with
9 satisfactory accuracy. Optimized EV charging stations based on the CMCLP model can remedy
10 the spatial mismatch between the EV demand and the existing charging station allocations. The
11 developed methodological framework is highly generalizable and can be extended to other regions
12 for EV charging demand estimation and optimal charging infrastructure siting.

13
14 **Keywords:** Electric vehicles, PageRank model, charging infrastructure optimization,
15 spatiotemporal travel patterns.
16

1 INTRODUCTION

2 With the incentives and policy support from governmental agencies and EV manufactures, EV
3 markets are progressively growing in the recent decade (1). EV sales reached to more than 2
4 million units globally in 2018 with an increase of 63% on a year-on-year basis (2). China and the
5 Unites States are the two major EV markets accounting for over 20% of the sales worldwide (3).
6 San Jose, San Francisco, and Los Angeles metropolitan areas, having some of the highest EV sales
7 and market shares, where there are already more than a quarter-million EVs on the roads (4). The
8 rapid growth of EV adoption results in the increase of charging demand as well. EV charging
9 events can be mainly divided into home charging, workplace charging, and public charging
10 depending on the locations (5). In 2010, ECOTality and Idaho National Laboratory conducted EV
11 charging units analysis (6). According to their result on 2,903 private EV owners in United States,
12 80% of charging events are conducted at the participants' home, and over 70% of the vehicles have
13 charged at locations other than home, such as shopping malls, restaurants, and work offices.
14 Therefore, effectively satisfying EV users' public charging needs is crucial. In fact, a recent study
15 shows that public charging infrastructure is a key to the growth of EV market (4). Another reason
16 for promoting public charging infrastructure is that although large portion of EV adopters in the
17 United States and Europe have home charging facilities, countries like China still have low
18 penetration of home charging due to fewer single-family dwellings. It is estimated that in China
19 public charging (as compared against home charging option) will increase from 55% to 80% by
20 2030 (7). Yet, two major barriers exist for most countries in terms of public charging infrastructure
21 expansion. First, some ill-chosen charging stations can be significantly underutilized due to their
22 inconvenience of access (e.g. distance). Distance plays an important role for EV users when
23 choosing charging stations because of range anxiety (8). Second, insufficient charging networks
24 in certain regions could fail to meet the charging demand (9). To this end, how to optimally allocate
25 the public charging stations to improve the charging coverage and effectively exploit their
26 utilization are the main challenges for siting public electric vehicle supply equipment (EVSE).

27 Solving EVSE allocation problem generally involves two steps: estimate spatial
28 distribution of charging demand; and apply mathematical modeling to obtain optimal locations
29 with specific objectives. When estimating charging demand, a common approach is to model the
30 EV battery usage, and simulate EVs' energy consumption under different traffic scenarios (10–
31 12). Such simulation-based approaches would be difficult to scale to large urban context due to
32 computational expense. In remedy to that, data-driven methodologies have gained more interests
33 in recent years with the proliferation of urban informatics and mobility data. For instance,
34 geographical features including point of interest (POI), traffic flow, and population density are
35 extracted as inputs to spatial statistical models to infer public charging demand (13, 14). Traffic
36 data such as GPS trajectory are available for exploring driver' travel patterns and further
37 identifying hot spots of large public charging demands. The general procedure for conducting such
38 type of analysis involves formulating it as a discrete problem by partitioning the study area into
39 sub-regions (or cells), extracting drivers' travel patterns from travel mobility data, and finally
40 inferring public charging demand for each cell (14-16). Yet, given that charging events usually
41 occur at the trips' destinations, it would be far-fetched to associate transient locations along one's
42 trip to the charging demand. Another issue with the existing charging demand estimation is the
43 lack of real-world data to either construct or validate the proposed models (13-14). Public charging
44 infrastructures are typically managed by governmental agencies or private companies, and the
45 charging event data are usually not publicly accessible.

1 To this end, this paper aims to develop an innovative approach leveraging PageRank
2 algorithm, graph theory, geographical features, and trajectory data to quantify the spatial
3 distribution of EV charging demand. PageRank algorithm is uniquely suited for this problem in
4 that it quantifies the importance of a web page via its linkage to other pages. Travel behavior to
5 certain extent resembles people's internet browsing process (treated as a random walk). While
6 PageRank algorithm is able to identify the important nodes within the graph topology, we develop
7 a modified geographical PageRank (MGPR), which is capable of incorporating geographical
8 features to estimate the EV charging demand within a region. The model validation is further built
9 upon an automated dynamic crawling pipeline for retrieving and storing the public charging
10 information. The estimated EV charging demand is then fused into a capacitated maximal coverage
11 location problem (CMCLP) model to optimize the EVSE distribution by maximizing the
12 utilization of charging stations. The framework is beneficial to transportation agencies and could
13 provide insightful guidance for future public EVSE installation.

14 **LITERATURE REVIEW**

15 **EV charging demand estimation**

16 A myriad of studies have utilized GPS trajectory data to explore trip purposes and spatiotemporal
17 travel patterns to infer EV charging demand. Hu et al. (17) used drivers' travel activities to evaluate
18 the feasibility of replacing the gasoline yellow taxi with BEVs in New York City. GPS data of
19 13,587 taxis spanning the entire year of 2013 were analyzed to extract spatiotemporal driving
20 patterns, travel demand, dwelling and other features. Their proposed BEV feasibility model
21 indicated that only 8% of current taxis can be freely charged under the constraints of mileage range
22 and pickup activity. Similarly, Tu et al. (18) employed optimization algorithm to optimize the
23 location of electric taxi in Shenzhen, China. Dynamic pickup demands were estimated using trip
24 data in combination with the corresponding transportation network information first, and then a
25 spatial-temporal demand coverage location model is applied to maximize the taxi service coverage
26 while minimizing the charging wait time. Their results indicate that downtown area, airport, and
27 railway stations have intensive charging demand for electric taxis. The aforementioned studies
28 offer insights on exploring the charging demand of electric taxis based on GPS data and trip
29 activity. However, travel patterns and charging demand can be drastically different between taxis
30 and private vehicles. Kontou et al. (16) explored the relationship between charging demand and
31 people's daily activities for private vehicles. They identified places with high trip destination
32 densities and prioritized those regions for charging infrastructure installation. The result showed
33 that if top 10% most frequently visited grid cells have installed charging stations in the Puget
34 Sound region, then EV users will be able to access public charging on 71% of their trips. This
35 study suggested that charging probability is highly associated with people's daily travel activities
36 and trip destinations. For EV drivers, they prefer to leave their EVs charging at nearby stations
37 while conducting other activities, e.g., working, shopping, etc. For people who plan to purchase
38 EV in the future, they are less willing to compromise their daily routines to go to distant charging
39 stations. Meanwhile, Vazifeh (15) reconstructed trajectory using cellular data to track individual
40 movement patterns in Boston area. A discrete optimization model is formulated by minimizing the
41 total number of charging stations and the average travel distance on those routes.

42 Apart from GPS trajectory data, urban informatics such as POIs are utilized to analyze the
43 charging demand. Wagner et al. (13) built a linear regression model using POIs to fit the usage
44 data from more than 32,000 charging sessions in Amsterdam. Results indicated that POI imposes
45 significant influence on the charging behavior of EV users. Likewise, Dong et al. (14) applied
46

1 spatial features including traffic flows, population density, and POI to model the charging demand
2 based on the distribution of current charging stations in London using Bayesian spatial log-
3 Gaussian Cox process model. Statistical analysis showed that transport, retail, and commercial
4 POIs significantly influence the charging demand in urban-scale region.

6 **PageRank model and its application**

7 PageRank is one of the most widely used web pages ranking algorithms, developed by Google
8 (19). PageRank model formulates the internet as a huge directed graph, where each website
9 represents a node and the hyperlinks are the edges connecting those nodes. Each node is assigned
10 a PageRank value, denoting the importance of the website. PageRank models users' internet
11 browsing behavior as a random walk process. The underlying assumption of PageRank is that more
12 popular web pages are likely to be linked from other web pages, and their importance tends to
13 propagate via hyperlinks. Nodes that are more frequently visited will receive higher PageRank
14 scores and are subsequently deemed more important. PageRank is proved to be extremely efficient
15 and simple enough to solve complex graph problems. Yet, a few strategies could be applied to
16 improve its performance. The original PageRank algorithm assumes that the transition probability
17 from one node to its all linked nodes is equal. However, that is not always the case in reality. For
18 example, it is likely that a user jumps to a more popular website over the less popular ones. To fix
19 this issue, Xing and Ghorbani (20) proposed a weighted PageRank algorithm. The core concept of
20 this extended model is to assign higher transition probability to more popular pages instead of
21 distributing equally. Another deficiency of the original PageRank is that it does not consider the
22 content of web pages. In many situations, users jump to other web pages with similar content.
23 Haveliwala (21) proposed a topic-sensitive PageRank algorithm by clustering the web pages into
24 a set of topics and biased the original PageRank with those topics. Such innovative idea makes it
25 possible for the PageRank model to incorporate more features for augmented model performance.

26 Although PageRank was originally used for ranking websites, it is quite effective to capture
27 a variety of relations among vertices of graphs (22). For instance, PageRank model has been
28 employed to infer traffic states in urban region. Kim et al. (23) explored the traffic congestion at
29 57 intersections in Cheongju city. Specifically, they generated a network graph to connect
30 intersections by roads, and then applied PageRank to extract intrinsic relationship of traffic
31 conditions across intersections. The result indicated that the intersections with higher PageRank
32 scores generally have higher traffic density and thus are prone to congestion. Wang et al. (24)
33 studied the traffic states in urban area of Beijing by partitioning the area into 62 by 65 grids and
34 constructing the network using 12,000 taxi GPS trajectories. The traffic volume between two
35 adjacent grids are used as the weight of the link. It is found that there exists a positive correlation
36 between the PageRank value and congestion index for most regions, and the PageRank value can
37 therefore predict the upcoming congestion. Besides the traffic states inference, PageRank model
38 has been applied to analyze other geographical-related problems, such as revealing urban structure
39 through roads connectivity (25).

40 To the best of our knowledge, PageRank model has not been utilized for EV charging
41 demand estimation to date. Yet, with the proliferation of big data (e.g. GPS trajectory, POI) as
42 reviewed in Section 2.1, PageRank is well suited for modeling EV charging demand from a graph-
43 theory perspective, as EV users travel from an origin and a destination can be treated as Markov
44 process, and the charging demand is highly correlated with the features of trip destinations (14).
45 A modified PageRank model not only can consider the EV users' travel habits for demand

1 estimation, but also can incorporate social dimension features (e.g. POI, land use) to improve
 2 model accuracy.

4 **Optimization of EVSE location**

5 Public charging infrastructure deployment problem can be deemed as optimally siting
 6 EVSE on a landscape. A variety of optimization algorithms have been employed to attempt this
 7 from multiple angles. Among them, maximal coverage location problem (MCLP) is a classic
 8 model to optimally assign facilities (26). Dong et al. (14) applied a standard MCLP to maximize
 9 the coverage of EV charging demand by assigning a fixed amount of charging stations. The model
 10 did not consider the constraint of charging stations' capacity, yet in reality charging stations are
 11 constrained by energy load. The CMCLP model is subsequently proposed to optimize EVSE
 12 location by taking into account the capacity constraints (27, 28). A more sophisticated approach
 13 to optimizing EVSE location is to formulate it as a multi-objective optimization problem. Wang
 14 and Wang (29) proposed a mixed integer programming model to site refueling stations to serve
 15 intercity and intra-city travel with the goals of minimizing siting cost and maximizing population
 16 coverage. Vazifeh et al. (15) treated this as a set covering problem with dual objectives of
 17 minimum number of charging stations required and minimum average distance for drivers to the
 18 nearest accessible charging stations. Extended upon that, Kınay et al. (30) developed a full cover
 19 modeling framework with a novel objective function, which optimizes the charging station
 20 locations and determines the optimal OD routes so that the total en-route recharging is minimal
 21 for each trip. Yet most of multi-objective optimization problems are computationally infeasible
 22 due to large amount of intricate constraints. Such optimization problems mostly require heuristic
 23 algorithms to obtain near-optimal solutions.

24 To this end, the CMCLP model appears to be computationally efficient and suited for the
 25 EV charging infrastructure allocation problem. The flexibility of having the capacity constraint is
 26 uniquely aligned with the EV charging problem, as agencies when siting the charging stations,
 27 have to consider the energy load capacity for the specific area. Further, CMCLP is not a binary
 28 allocation, in that the model allows partial charging demand assignment. In case where one
 29 charging station reaches its capacity, the rest of the charging demand can be allocated to another
 30 eligible station nearby.

32 **METHODOLOGY**

33 In this section, a proposed MGPR model is presented, followed by the formulation of
 34 CMCLP optimization model. PageRank is uniquely suited for this study, as we partition the entire
 35 study area into grid cells. We further extract the spatial correlation built off of trips' origins and
 36 destinations (OD) and associate that with potential charging demand. The problem as such can be
 37 treated as a directed graph, where each grid or cell within the study area is treated as a node and
 38 can be characterized by the PageRank score, describes how appealing that cell is to the EV users.
 39 *Modified geographical PageRank (MGPR) model*

40 Given a weighed directed graph $G = (V, E, W)$, where V represents the set of nodes, E
 41 represents the set of edges, and W is the set of weight corresponding to each edge. The simplified
 42 version of PageRank model is defined as follows:

$$43 \mathbf{R}_{t+1} = \mathbf{M}\mathbf{R}_t \quad (1)$$

44 where \mathbf{R}_t is the vector indicating the PageRank value of each node at step t . Formally, $\mathbf{R}_t =$
 45 $[PR(v_1), \dots, PR(v_n)]^T$, and n is the total number of nodes. \mathbf{M} is the stochastic matrix that describes

1 the transition probability from one node to another. For each node j , the transition probability has
 2 the following two properties:

$$3 \quad M_{ij} \geq 0 \quad (2)$$

$$4 \quad \sum_{i=1}^n M_{ij} = 1 \quad (3)$$

5 After infinite steps of long walk, the PageRank value for each node will converge to a stationary
 6 probability denoted by the following equation:

$$7 \quad \mathbf{MR} = \mathbf{R} \quad (4)$$

8 To guarantee convergence, the graph is required to be a strongly connected graph, and an
 9 aperiodic one. However, not all network graphs can meet the aforementioned requirements. To
 10 address this problem, the simplified PageRank incorporates a random term to make the graph
 11 strongly connected and aperiodic. Eq. (4) is therefore modified as follows:

$$12 \quad \mathbf{R} = d\mathbf{MR} + \frac{(1-d)}{n} \mathbf{1} \quad (5)$$

13 where the second term allows each node has a certain probability to transfer to all other nodes, and
 14 d is the damping factor that controls the tradeoff between the first and the second terms.

15 In the original PageRank model, the network graph does not consider the weight of links.
 16 Instead, it assumes all links have equal transition probabilities. Specifically, for node j , M_{ij} shares
 17 equal transition probability for each incoming node i , if there is an edge between nodes i and j , and
 18 otherwise 0. As noted by Kontou et al. (16), trip destination density can be used as a surrogate to
 19 measure potential EV charging demand. Therefore, in the MGPR, instead of assuming equal
 20 transition probability across nodes, we use the trip counts (derived from vehicle trajectories) to
 21 construct the transition matrix. The transitional probability M_{ij} is thus re-defined as:

$$22 \quad M_{ij} = \frac{w_{ij}}{\sum_{i=1}^n w_{ij}} \quad (6)$$

23 where w_{ij} is the trip count from node i to node j . Another flaw of the original PageRank is the
 24 inability to incorporate other information such as web content. Inspired by the topic-sensitive
 25 PageRank algorithm (21), we adopted similar concept to our proposed model such that social
 26 dimension that might influence the EV charging demand could be incorporated. The core idea is
 27 to add a third term in the PageRank model. Different from the second term in Eq. (5) which has
 28 equal transition probability to all nodes, the third term will direct the drivers to other nodes with
 29 varying probabilities. Grid cells that are more favorable to charging activities would receive higher
 30 transitional probabilities. For instance, if a grid cell contains large number of commercial buildings,
 31 EV drivers are more likely to charge in that cell during the day (while they work). The proposed
 32 MGPR model is presented below:

$$33 \quad \mathbf{R} = \alpha_1 \mathbf{MR} + \frac{\alpha_2}{n} \mathbf{1} + \alpha_3 \mathbf{G} \quad (7)$$

34 where \mathbf{G} represents the social dimension term, α_1 , α_2 , and α_3 are the weights of PageRank term,
 35 random transferring term, and social dimension term, respectively. The sum of α_1 , α_2 , and α_3
 36 should equal to 1. In this study, POI data, land-use type information, and socio-economic factors
 37 are used to describe urban and geographical features. The social dimension term \mathbf{G} is therefore
 38 defined as:

$$39 \quad \mathbf{G} = \frac{1}{3} (\mathbf{G}_{POI} + \mathbf{G}_{land-use} + \mathbf{G}_{socio-economics}) \quad (8)$$

1 Detailed information and definition with respect to the social dimension features will be introduced
 2 in the *Data* and *Results* sections.

3 *CMCLP optimization model*

4 In this study, we formulate the optimal public EVSE allocation problem as CMCLP
 5 following similar ideas from (27, 28). The mathematical formulation is defined as follows:

6 Objective function:

$$7 \quad \text{Maximize } \sum_i \sum_{j \in N_i} Z_{ij} \quad (9)$$

8 Subject to:

$$9 \quad \sum_j Z_{ij} \leq a_i, \forall i \quad (10)$$

$$10 \quad \sum_j X_j = p \quad (11)$$

$$11 \quad \sum_i Z_{ij} \leq c_j X_j, \forall j \quad (12)$$

$$12 \quad X_j = \{0,1\}, \forall j \quad (13)$$

13 where

14 i is the index of grid cells

15 j is the index of candidate grid cells that can be assigned with new charging stations

16 Z_{ij} indicates the amount of charging demand that can be covered in grid i by the
 17 neighboring charging stations j

$$18 \quad X_j = \begin{cases} 1; & \text{if charging station } j \text{ is sited} \\ 0; & \text{otherwise} \end{cases}$$

19 a_i is the estimated charging demand in each grid i

20 N_i is the set of potential neighboring charging stations for grid cell i

21 c is the capacity of each charging station

22 p is the total number of charging stations

23 The objective function Eq. (9) is maximizing the coverage of charging demand for all grids.

24 Constraint (10) guarantees the charging energy provided by neighboring charging stations is under
 25 the estimated charging demand for grid i . Constraint (11) defines the total number of charging
 26 stations that are planned to be installed in the study area. Constraint (12) defines that the allowed
 27 charging energy each charging station serves to the neighboring area cannot be greater than its
 28 capacity. Constraint (13) ensures X_j is a binary variable. According to Prianka (31), the willingness
 29 of people walking from parking location to their activity place would become extremely low when
 30 the distance is over 3,000 feet (0.91 km). For this reason, we define that the neighboring charging
 31 stations for a grid cell refer to charging stations located in its adjacent 8-directional grid cells. The
 32 CMCLP is solved using a commercial optimization solver Gurobi in this study.

33

34 **DATA PROCESSING AND ANALYTICS**

35 **Data**

36 *OD data*

37 As noted earlier, in order to apply the MGPR to inferring charging demand, the problem is treated
 38 as a directed graph, where each grid cell within the study area is treated as a node and the edge is
 39 characterized by the number of trip ODs. The OD data are obtained from probe vehicle trajectories
 40 provided by Inrix. The trajectories were extracted from a portion of vehicle stream using probe
 41 sensors, such as cell phone and automated vehicle location (AVL). The raw data contains 2.5
 42 million trips distributed in the State of Utah during September of 2018. We further filtered the trips

1 that are enclosed within the Salt Lake City metropolitan area, as it is the boundary of this study.
 2 As described in Section 3, we employ a grid-based approach to partition the region and modeling
 3 the EV charging demand. Such level of granularity can remedy the GPS reading errors, while
 4 providing sufficient resolution for EVSE planning purpose. Note that determining the size of grid
 5 cells is an empirical process. If the size is set too large, it would be difficult to pinpoint the optimal
 6 locations of charging stations with fine granularity. On the contrary, small grid cell size may lead
 7 to failure in capturing hot spots of high charging demand. Previous studies (14, 16, 18) suggest the
 8 appropriate size of grid cells set as 1km by 1km. After grid segmentation, there are 756,303 trip
 9 OD pairs in total within the region. The maximum number of origin count in a grid cell is 9,281,
 10 and the maximum number of destination count in a grid cell is 9,268.

11 *POI data*

13 POI data can effectively represent urban context and infer people’s trip purposes (13). In this study,
 14 we use Google Place API to extract POIs in our study area. There are 62,673 POIs in total obtained
 15 from Google Place API with 103 different labels. In fact, many labels share similar denotation.
 16 For instance, both hospital and doctor refer to health-related POI. For simplicity and practical
 17 concerns, we further classify the 103 labels into 11 categories. The detailed information of
 18 classified POI data is shown in Table 1.

19
 20 **TABLE 1 Description of POI Data**

POI ID	Category	Label Examples	Total Number
1	Business	office, personal business	23,472
2	Health	hospital, health, doctor	8,982
3	Finance	agency, finance building	6,691
4	Retail	supermarket, grocery store	10,066
5	Restaurant	restaurant, food delivery	2,181
6	Transportation	bus station, train station	3,140
7	Education	school, university	1,290
8	NGO	church, government building	1,591
9	Entertainments	park, salon, bar ,zoo	2,422
10	Service	post office, gas station, laundry	2,427
11	Hotel	hotel, lodging	410

21
 22 Among the eleven categories, a few do not have apparent association with public charging
 23 behaviors. To reduce the noise that might be incurred, Health, NGO, and Service POIs are
 24 eliminated for further analysis.

25 *Social dimension features*

26 Socioeconomics describes the relationship between social behavior and economics, while land-
 27 use information reveals the human use of land. These two types of geographical-based features are
 28 highly associated with people’s parking behaviors and subsequently could impact the potential EV
 29 charging demand (9). For this reason, we incorporate socioeconomic and land use features in our
 30 model to infer the public charging need. These two datasets are obtained from Wasatch Front
 31 Regional Council (WFRC), the metropolitan planning organization that synthesizes a variety of
 32 data sources for transportation planning in the region. Population data is obtained at traffic analysis
 33 zone (TAZ) level. Land-use is categorized into agriculture, commercial area, residential area,
 34

1 recreation, and transportation. For simplicity, we reclassified the land-use into commercial vs. non-
 2 commercial region only, since most public charging facilities are inclined to be installed in
 3 commercial places.

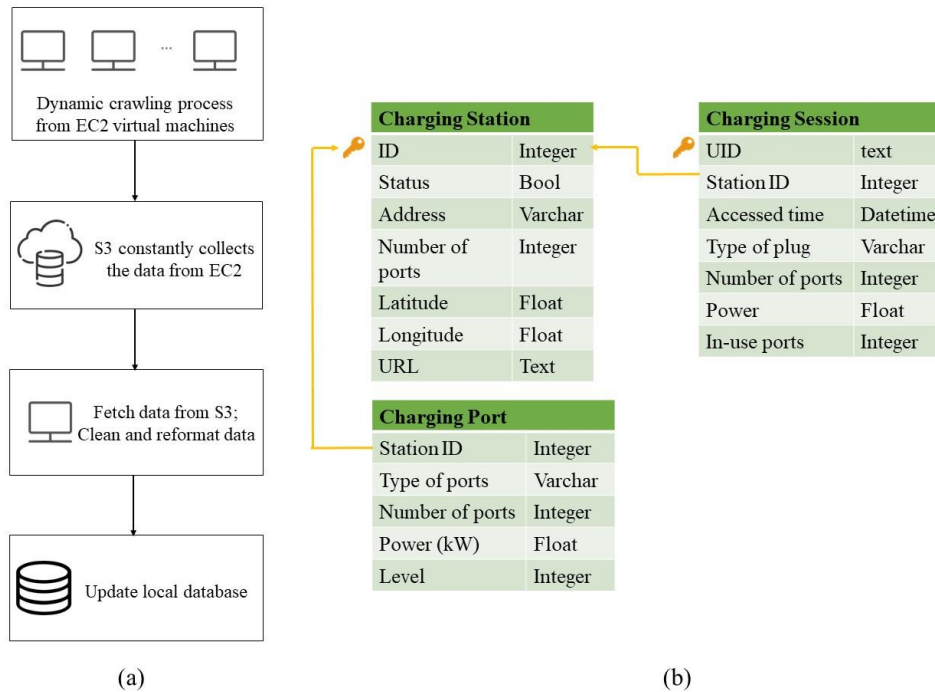
4 *Real-world public charging data*

5 The real-world charging data is crawled from ChargePoint, an online application that assist EV
 6 users navigate and review nearby charging sites. ChargePoint operates the largest online network
 7 of independently owned EV charging stations, operating in 14 countries worldwide. Directly
 8 accessing the utilization information of public EV charging stations is challenging, since it requires
 9 the authorization from owners of EVSE. Alternatively, such information can be accessed via
 10 Google Map Service. We search all public charging stations in the study area first, and then retrieve
 11 the real-time data (e.g. the number of in-use port) constantly for each charging station. Meanwhile,
 12 associated features (e.g. power, location) for each charging station are collected. There are 126
 13 public charging stations with 576 charging ports recorded by ChargePoint in the Salt Lake City
 14 metropolitan area. Among them, 109 charging stations (516 ports) broadcast real-time utilization
 15 information (i.e. number of in-use port at current time point), indicating charging status. A sample
 16 of collected features of public charging stations is displayed in Table 2.

17
 18
 19 **TABLE 2 A sample of Stationary Features of Five Public Charging Stations**

Station ID	Number of Port	Address	Latitude	Longitude	Power of Port (kW)	Status
0	2	425S Orchard Dr, North SLC	40.83**	-111.91**	7.2	Available
1	4	2280 Rose Park Ln, SLC	40.77**	-111.94**	7.2	Unknown
2	2	210N 1950W, SLC	40.77**	-111.94**	7.2	Available
3	8	168 N 1950 W, SLC	40.77**	-111.94**	7.2	Available
4	6	195 N 1950 W, SLC	40.77**	-111.95**	7.2	Available

20
 21 In order to obtain the real-time charging station utilization, we applied *beautifulsoup*
 22 package in Python, which is a package for crawling on HTML. The program is further deployed
 23 on Amazon Web Service (AWS) Elastic Compute Cloud (EC2) and Simple Storage Service (S3)
 24 for dynamic crawling. The dynamic crawling framework and schemas of database are displayed
 25 in Figure. 1(a) and (b), separately. Three virtual machines were rented on EC2 to cover all charging
 26 stations in the study area, and the crawling was triggered every 10-minute for each charging station.
 27 The data collection spanned from Nov 5th, 2020 to Dec 12th, 2020. The dataset contains 656,179
 28 records for the 109 charging stations.

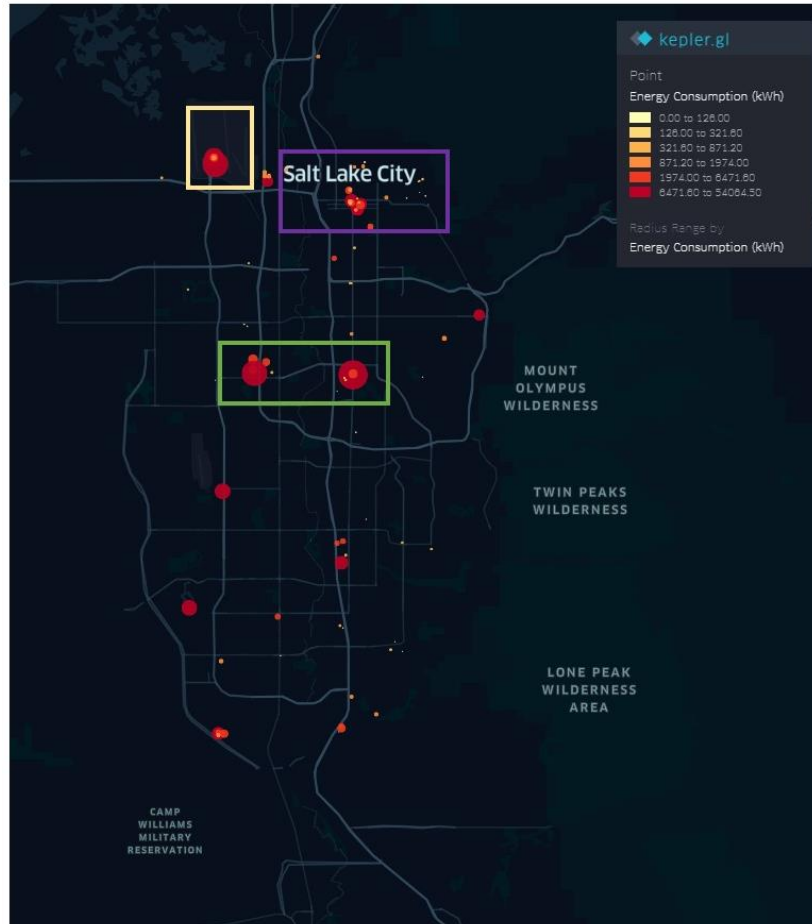


1
2 **Figure 1 (a) Framework of dynamic crawling; and (b) the SQL schema for the database of**
3 **EV charging information**

4
5 There are three tables in our database to store the public charging data, as shown in Figure.
6 1(b). *Charging Station* and *Charging Port* tables record the associated features for charging
7 stations and corresponding charging ports. *Charging Session* table documents the dynamic
8 crawling records. The *in-use ports* feature reflects the number of ports being occupied at a charging
9 station at a specific time point. We further aggregated the crawled records to obtain the charging
10 energy at each station. In a nutshell, once the crawler detects that the charging ports in a station
11 are in use, the energy consumption at that time point is calculated as the total number of in-use
12 ports multiplied by the corresponding power of the port and 0.167 hour (the crawling interval).
13 The accumulative energy consumption is then summed up across entire crawling period as the
14 total charging energy consumption.

15
16 **Spatiotemporal Analysis**

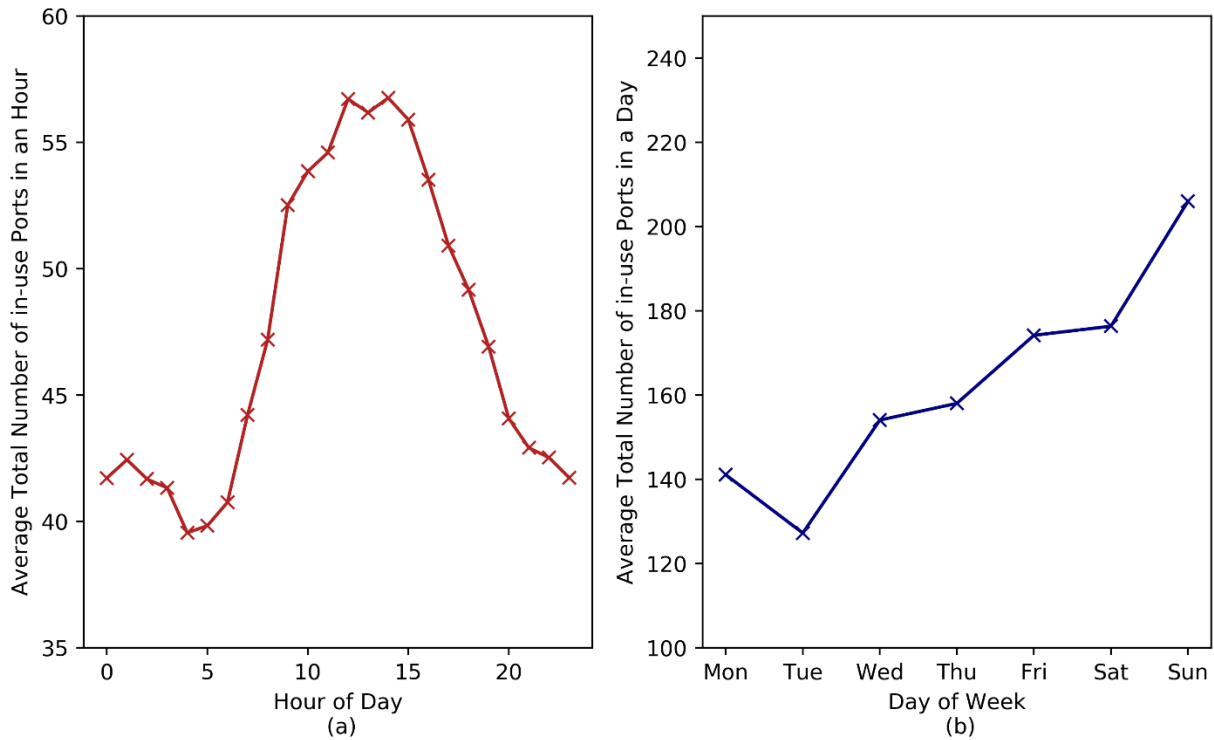
17 We examine the spatiotemporal distribution of the charging energy consumption based on the data
18 collected. Figure. 2 indicates the accumulative energy consumption at each charging station within
19 the study period.



1
2 **Figure 2 Total energy consumption of each public charging stations across entire period**

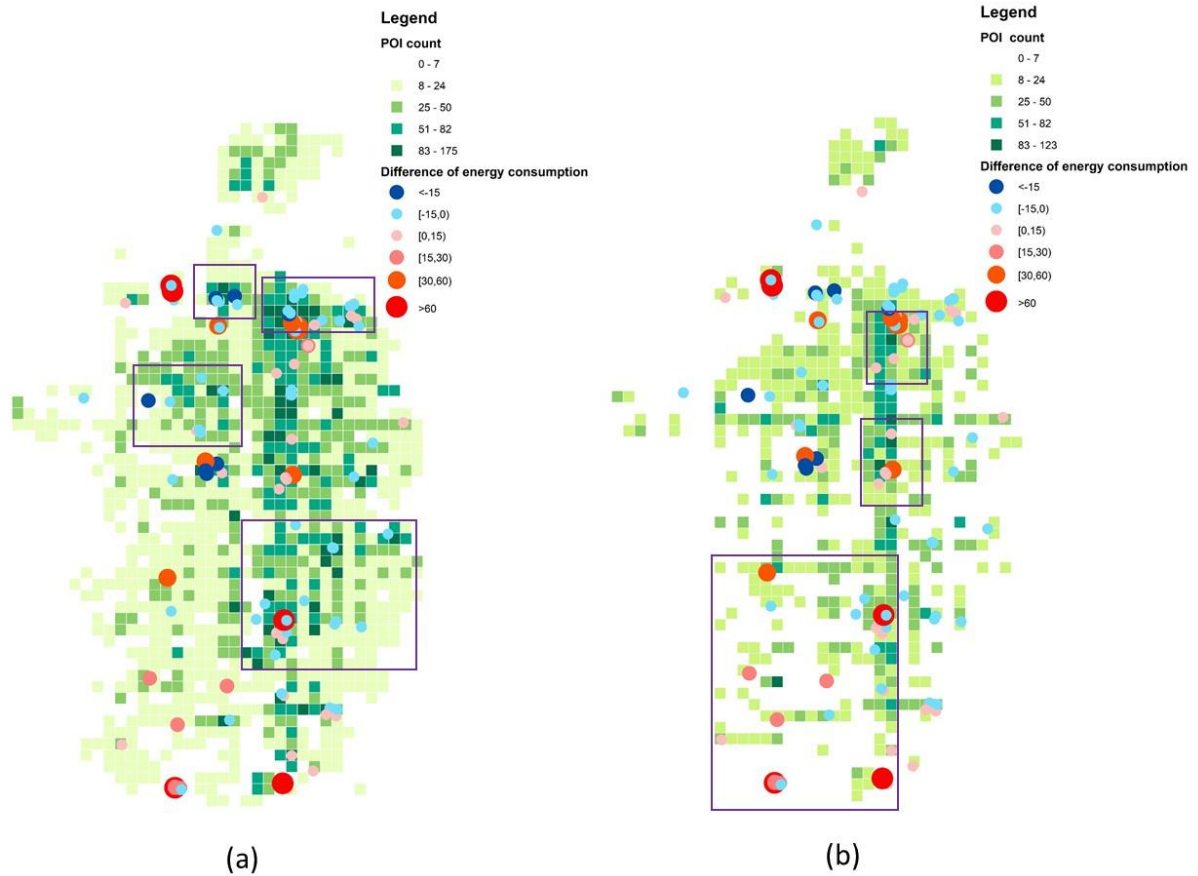
3
4 In Figure. 2, two charging stations highlighted by green show very high energy
5 consumption. These two charging stations are equipped with Level 3 charging ports (CSS and
6 CHAdeMO) which have much higher power than level 2 ports. The energy consumptions are
7 therefore larger. A cluster of charging stations with high demand exist around the Salt Lake City
8 downtown area (marked by purple). Although none of them exhibit extremely large energy
9 consumption, the average usage frequency is relatively high compared to stations in other areas. It
10 is worthy to note that the Salt Lake City international airport (marked by yellow) indicates high
11 energy consumption as well. EV users might charge their vehicles while waiting to pick up
12 someone or travel to other places while leaving their vehicles charged at the airport.

13 We further aggregate the charging station utilization data by different time resolutions to
14 examine the temporal patterns. Figure. 3(a) shows that most of the charging activities occur during
15 the day, between 7:00 am to 7:00 pm. Figure. 3(b) indicates that the average charging demand on
16 Monday and Tuesday is relatively low, while the highest charging demand is observed on Sunday.
17 There is a significant difference between charging patterns across the day-of-week. The average
18 number of daily in-use port is 145 Monday through Thursday, and 185 Friday through Sunday.



1
2 **Figure 3 (a) The average total number of in-use ports in each hour of day; and (b) the average**
3 **total number of in-use ports in each day of week**

4
5 Subsequently, we explore the difference of charging patterns by day-of-week. Specifically,
6 for each station, we calculate the difference between the average daily charging energy
7 consumption from Friday to Sunday and that value from Monday to Thursday. In fact, charging
8 behaviors during Monday to Thursday are more likely to be linked with work trips, while charging
9 behaviors during Friday to Sunday are more likely to be linked with non-work trips. We further
10 overlay the POI data to infer the nature of trip purposes around the charging stations. For POI data,
11 we combine the finance, business, and education into one group to infer work trips. Retail,
12 entertainment, and restaurant POIs are grouped together to infer the non-work trips. The charging
13 differences by day-of-week (i.e. average daily charging energy consumption from Friday to
14 Sunday minus that value from Monday to Thursday) are presented under different POI types in
15 Figure. 4 (a) and (b), respectively.



1
2 **Figure 4 (a) The work-related POIs (financial buildings, business, and education)**
3 **distribution and public charging stations' charging patterns; (b) the non-work-related POIs**
4 **(entertainment places, retails, and restaurants) distribution and public charging stations'**
5 **charging patterns**
6

7 In Figure. 4(a), it is found that charging stations that are more frequently used during
8 weekdays are located around regions with large number of POIs associated with workplace. In
9 contrast, charging stations that are more frequently used during weekends are mostly scattered in
10 remote regions away from downtown as shown in Figure. 4(b). POIs such as parks, grocery stores
11 are identified in neighboring regions. This distinction of charging patterns with respect to day-of-
12 week validates the aforementioned hypothesis. Note that the Salt Lake City downtown area is
13 mixed land use with both commercial buildings and recreational places. As a result, there is a mix
14 of usage both on weekdays and weekends.
15

16 **RESULT AND ANALYSIS**

17 **PageRank model**

18 In our proposed MGPR model, the OD matrix M is defined in Eq. (6). The social dimension term
19 G includes G_{POI} , $G_{socio-economics}$, and $G_{land-use}$. G_{POI} for grid cell i is calculated as the number
20 of POIs in the grid cell i divided by the total number of POIs in study area. Similarly, population
21 density for grid cell i is calculated to represent $G_{socio-economics}$ value for grid cell i . Lastly,
22 dummy variable is used to indicate whether grid cell i is a commercial area. The dummy value is

1 then normalized to represent $G_{land-use}$ value for grid cell i . The coefficients α_1 , α_2 , and α_3
 2 control the OD matrix, random effect, and social dimension, respectively. For example, large
 3 α_1 will cause OD matrix dominates PageRank score. In this study, the parameter values are
 4 determined empirically. α_2 is set as 0.05 since random effect is expected to be marginal.
 5 Meanwhile, it is found that when α_1 ranges between 0.5 and 0.7, no much variation on results is
 6 detected. The optimal result is observed when α_1 , α_2 , and α_3 are set as 0.6, 0.05, and 0.35,
 7 separately. Once the coefficients are determined, PageRank value is determined via an iterative
 8 process. We keep updating the PageRank vector R_t in Eq. (7) at each step t until it reaches
 9 convergence. The total number of iteration steps is set as 500 for the MGPR. Numeric result
 10 indicates that when the step reaches 20, the PageRank value almost converges.

11 To test the effectiveness of our proposed model, the original PageRank model and weighted
 12 PageRank model are also developed for comparison purpose. For original PageRank and weighted
 13 PageRank models, we adopt 0.85 for the dampening factor d in Eq. (5) as seen in (19, 20). The
 14 computation of PageRank values for original PageRank and weighted PageRank models follows
 15 similar process. In order to quantify model performances, the following two metrics are used:

16 **Weighted total energy (WTE):** the weighted total energy is defined as follows:

$$17 \quad WTE = \sum_{i \in S} R_i * d_i \quad (14)$$

18 where S is the set of grid cells with charging facilities; R_i is the normalized PageRank value of the
 19 i^{th} grid cell, and d_i is the actual charging energy of the i^{th} grid cell. It measures the ability of the
 20 model to capture paramount charging demand regions. If the normalized PageRank values of grid
 21 cells with large charging energy are high, WTE would be large as well.

22 **Mean absolute rank difference (MARD):** MARD is calculated by averaging the absolute
 23 difference of the rank of PageRank value and the rank of actual charging energy for each grid cell
 24 equipped with charging facilities. It is expressed as follows:

$$25 \quad MARD = \frac{1}{N} \sum_{i \in S} |Rank_{R_i} - Rank_{d_i}| \quad (15)$$

26 where N is the total number of grid cells with EVSE; $Rank_{R_i}$ is the ranking of PageRank value
 27 for the i^{th} grid cell, and $Rank_{d_i}$ is the ranking of actual charging energy consumption for the i^{th}
 28 grid cell. The smaller MARD is, the better the result is. MARD value reflects how well the model
 29 can distinguish high and low charging demand regions. Additionally, a random scenario, where
 30 each grid has equal PageRank value ($1/N$), is added to benchmark the PageRank models. The
 31 results of all models are shown in Table 3.

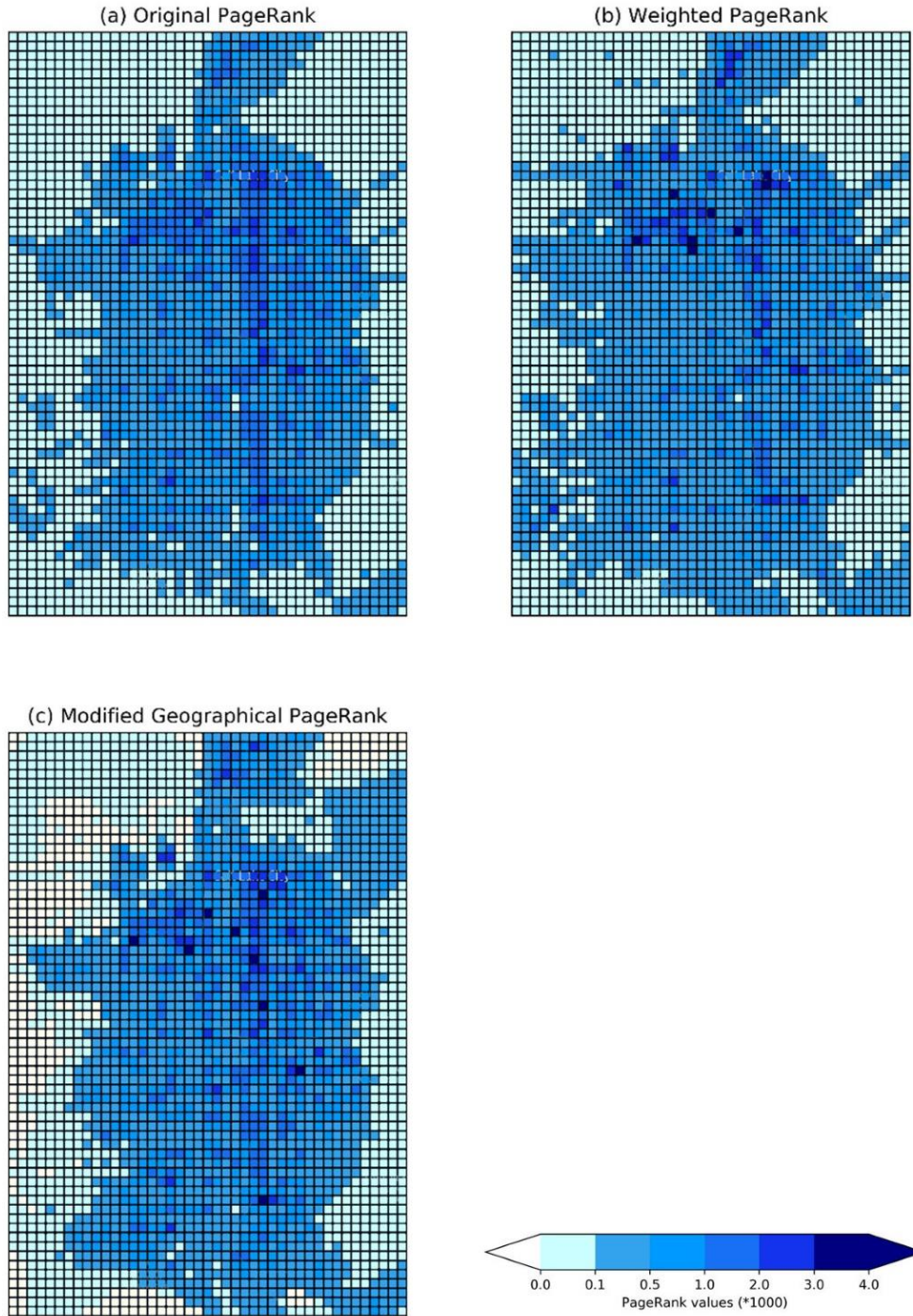
32
 33 **TABLE 3 The WTE and MARD Values for Original PageRank, Weighted PageRank, and MGPR**
 34 **Models**

Metrics	Random Scenario	PageRank	Weighted PageRank	MGPR
WTE	92.0	444.1	550.2	630.0
MARD	NA	18.8	18.2	11.8

35
 36 In Table 3, it is observed that WTE has a substantial increase over the random scenario by
 37 using original PageRank model. Such result indicates that trip count can imply EV charging
 38 demand effectively in urbanized area. Compared to original PageRank model, the weighted
 39 PageRank increases WTE value by 106.1, suggesting that trip density of each OD grid pair should
 40 be taken into consideration. Moreover, the MGPR further augments the model performance with

1 WTE value of 630. One possible explanation is that social dimension features such as the number
2 and type of POIs reflect trip purposes that are associated with public charging behaviors. Note that
3 in random scenario, all grid cells share same PageRank value and same rank, hence the MARD
4 value cannot be computed. As for the original PageRank and weighted PageRank model, the
5 MARDs are relatively close and much higher than MARD for MGPR. The significant reduction
6 of MARD by incorporating social dimension features illustrates that for some of regions with high
7 trip density their charging demands are not necessarily high, e.g., residential neighborhoods. To
8 better visualize the results geographically, we present the grid plot for each model, separately, in
9 Figure. 5.

Under Review



1
2 **Figure 5 (a) PageRank values distribution of original PageRank model; (b) weighted**
3 **PageRank model; and (c) MGPR model**
4

5 The original PageRank and weighted PageRank indicate similar public charging demand
6 distributions as illustrated in Figure. 5(a) and (b). However, some cells receive higher PageRank
7 values by employing weighted PageRank. Those cells have higher trip density, and subsequently

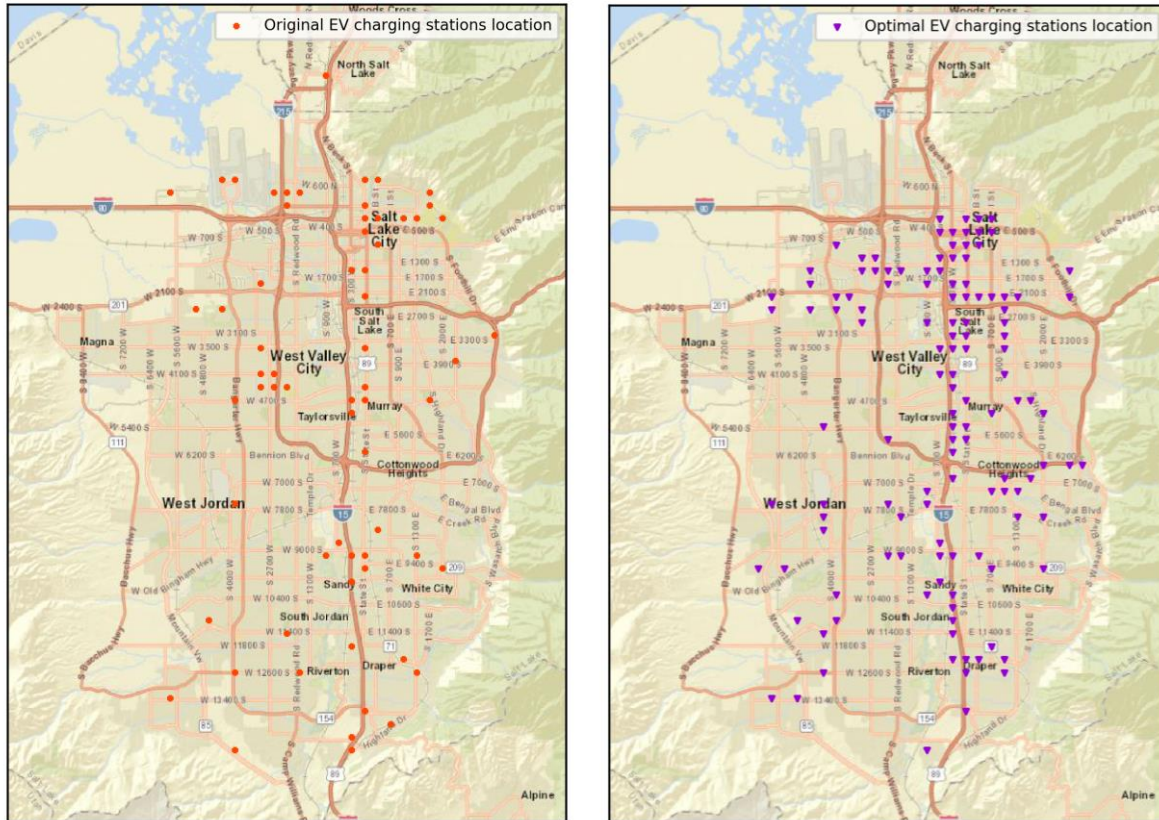
1 more appealing to charging activities. In Figure. 5(c), it is observed that the PageRank values of
2 large portion of cells located in the outskirts decrease to 0. We also notice that the PageRank values
3 for some cells increase on the contrary, which is attributable to the POIs, population density, and
4 land-use type. In summary, MGPR presents a more distinct pattern compared to original PageRank,
5 and Weighted PageRank.

7 **Optimizing public charging stations**

8 As indicated by WTE and MARD in Section 5.1, the MGPR model can effectively quantify EV
9 charging demand using PageRank score. With the real charging energy data collected, one can
10 build a model to map the PageRank score to the charging energy consumption for each grid. In
11 this study, 63 grid cells that contains the ground truth EV charging energy consumption are utilized
12 to build a regression model. Specifically, the regression model is defined as follows:

$$13 \quad y = \max(0, \beta_1 x_1^2 + \beta_2 x_2 + \beta_0) \quad (16)$$

14 where y is the daily estimated charging energy (kwh) in a grid cell; x_1 and x_2 denote the
15 normalized PageRank value and the number of charging ports in that grid cell, respectively; β_0 ,
16 β_1 and β_2 are corresponding coefficients. The least square method is applied to obtain the
17 estimated coefficients, where the values of β_0 , β_1 and β_2 are -107.73, 1.25×10^7 , and 15.46,
18 respectively. The value of R^2 being 0.78 indicates a satisfactory model fitness. We then use this
19 model to estimate the charging demand at each grid cell and Figure 6 (a) shows its spatial
20 distribution and the demand coverage of existing 126 charging stations. The total potential
21 charging demand in Salt Lake City metropolitan area is estimated as 11.89×10^4 kWh, and the
22 existing 126 charging stations can only supply 1.58×10^4 kWh energy, which is 13.3% of the total
23 public charging demand in the Salt Lake City metropolitan area.



(a)

(b)

Figure 6 (a) Existing allocation of public EV charging stations; and (b) optimal allocation of public EV charging stations

Given the estimated charging demand across the region, we can further explore the optimal siting of public charging stations by employing the CMCLP optimization model. While there are 2,816 grid cells, not all grid cells are suitable for siting new public charging stations due to their unique land-use types. We assume that the new public charging stations can be only installed in grids with public parking lots. The public parking lots data is available from WFRC, and there are 463 grid cells in total with public parking lots as shown in Figure. 7. Meanwhile, for those grid cells that are currently not equipped with charging stations, the number of charging ports x_2 is unavailable. Without loss of generality, we assume each grid cell is allowed to install at most one public charging station. Each charging station is equipped with four 7.2kW charging ports, and the capacity constraint for each port is set as 57.6 kWh.

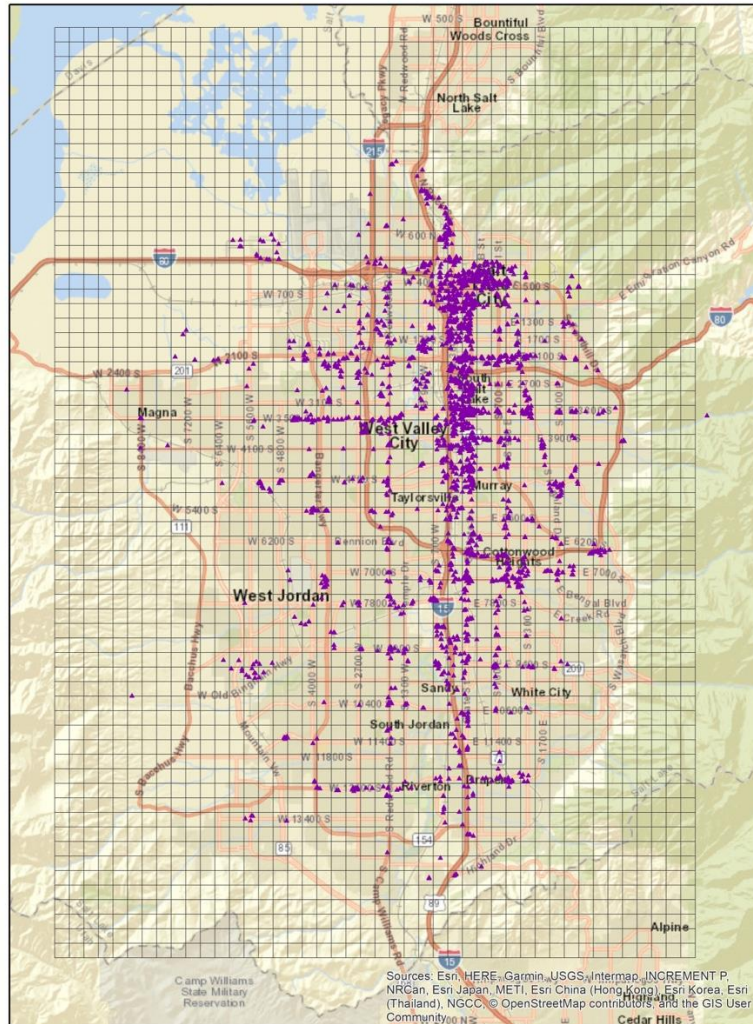
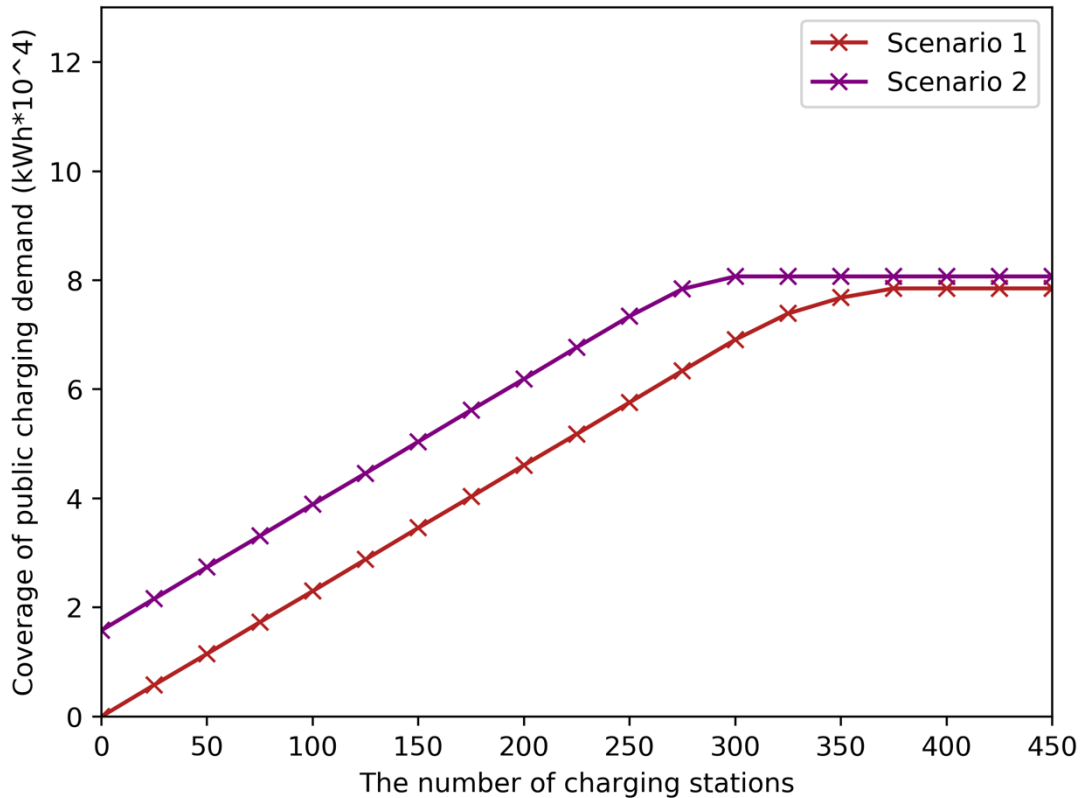


Figure 7 The distribution of public parking lots in the Salt Lake City metropolitan area

The CMCLP is solved for various potential values of p (number of charging stations to site) using Gurobi to explore the tradeoff between the cost of building charging stations and the service coverage of charging demand. Figure. 8 shows the tradeoff curve, where Scenario 1 assumes that there is no existing public EV charging station prior to optimization. As shown from the curve, clearly the coverage of charging demand increases linearly as the number of charging stations increases from 1 to 300. However, the growth rate decreases after $p = 300$, indicating that some of the additional charging stations are not fully utilized. The maximum service coverage is reached when the number of sited charging stations is 370 ($p=370$). No more charging stations can lead to increased service coverage. It is also important to note that 126 sited charging stations can provide service for 24.4% of charging demand in Salt Lake City metropolitan area. This is a significant demand coverage increase compared with 13.3% service coverage provided by the existing 126 charging stations, suggesting that these newly planned sites can serve EVs more effectively. These newly planned 126 sites are shown in Figure. 6 (b). It is observed that the optimally allocated charging stations are clustered in Salt Lake City downtown (northeastern), indicating large charging demand in that area. In fact, a large portion of current charging stations are deployed in downtown already. Such result suggests that most of charging stations in this region are effectively

1 exploited. Yet there are areas (e.g. West Valley) where a congregated number of EVSEs are
 2 currently present that might need to be reallocated. One possible explanation is that those EVSEs
 3 are located in residential neighborhoods where people can just charge their EVs at home instead.
 4 Another observation is that many optimal charging stations are distributed along the freeways,
 5 such as I-15. Chen et al. (2016) mentioned that freeways generally have excessive vehicle flow
 6 and correspondingly high quick-charging demand. Future deployment of public charging stations
 7 can be considered to be located in the close vicinity of freeway entrance or exit.



8
 9 **Figure 8 Total charging demand coverage under different number of public charging**
 10 **stations**

11 In addition, we explore where to site new charging stations to maximize the service
 12 coverage of charging demand given the existing 126 charging stations. Such tradeoff curve
 13 between demand coverage and number of sited charging stations is displayed in Figure. 8 (Scenario
 14 2). The demand coverage reaches its peak at $p=300$, providing service to 67.9% of charging
 15 demand in Salt Lake City Metropolitan Area.

16
 17 **CONCLUSION**

18 In this paper, we present a methodological framework for EV charging demand estimation and
 19 EVSE re-allocation using advanced graph-theory based approach and mathematical modeling.
 20 First, we developed a MGPR model based on the classic web ranking algorithm-PageRank-to
 21 explore potential charging demand by translating the problem into a directed graph and utilizing
 22 trip ODs and social dimension features. Second, an optimization model CMCLP is employed to
 23 optimize the locations of EVSEs by maximizing the utilization of charging stations. In addition, a

1 crawling pipeline is created to retrieve real-world public charging data for modeling purpose. Such
2 pipeline framework can be widely generalizable to other cities covered by ChargePoint.

3 The Salt Lake City metropolitan area is chosen to demonstrate the effectiveness of the
4 framework. Real-world data were obtained from 109 public charging stations from Nov 5th, 2020
5 to Dec 12th, 2020. Both WTE and MARD values indicate satisfactory performance of MGPR
6 model, which proves that trip ODs and social dimension features can effectively infer the public
7 charging demand. Once charging demand distribution is obtained based on the PageRank score
8 integrated regression model, CMCLP is employed to optimize the EVSE locations. It is found that
9 most of existing charging stations located at Salt Lake City downtown are effectively exploited;
10 while some charging stations located in West Valley City are underused. Meanwhile, it is observed
11 that there are mismatches between the currently deployed charging infrastructures and charging
12 demand. More charging stations are encouraged to be sited along the interstate highways for future
13 planning. We further examine the public charging demand coverage rate with the increase of
14 EVSEs. The numerical results indicate that the currently installed charging stations can only cover
15 13.3% of the total charging demand in Salt Lake City metropolitan area. With 300 more newly
16 sited charging stations at public parking lots, the coverage rate can reach to 67.9%. In the CMCLP
17 model, considering the small amount of Level 3 charging stations (34 out of 576), we simplified
18 the scenarios by assuming all charging stations are Level 2. However, several cities such as Los
19 Angeles have much higher proportion of Level 3 charging. Future work therefore includes
20 incorporating additional constraints to distinguish Level 2 and Level 3 charging stations.

21 **AUTHORS CONTRIBUTION**

22 The authors confirm contribution to the paper as follows: study conception and design: ZY, XCL,
23 RW; data collection: ZY, XCL, RW; analysis and interpretation of results: ZY, XCL, RW; draft
24 manuscript preparation: ZY, XCL, RW, YZ. All authors reviewed the results and approved the
25 final version of the manuscript.
26
27

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